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Turbulent transport and evolution of kappa distribution in the plasma sheet

M. Stepanova

Universidad de Santiago de Chile

E.E. Antonova

Lomonosov Moscow State University

Main unsolved questions:

- What do we know about the thermalization of collisionless space plasmas?
- What do we know about the turbulent transport?

Kappa distribution in Space Plasmas

First introduced by Montgomery in 1965

$$f(E) = \frac{n}{\pi^{3/2} E_c^{3/2} \kappa^{3/2}} \frac{\Gamma(\kappa + 1)}{\Gamma(\kappa - 1/2)} \left[1 + \frac{E}{\kappa E_c} \right]^{-\kappa-1} \quad (1)$$

where n is the particle density, E is the particle energy, E_c is the particle characteristic energy, Γ is the Euler gamma function, and κ is the spectral index characterizing the electron (ion) distribution.

For $\kappa \rightarrow \infty$ (1), tends to the Maxwellian distribution:

$$f(E) = \frac{n}{\pi^{3/2} E_c^{3/2}} \exp \left[-\frac{E}{E_c} \right] \quad (2)$$

It is widely used for systems out of thermal equilibrium

In space and astrophysical plasmas:

Collier, 1993; Tsallis et al., 1998; Tsallis, 1988; Treumann, 1999a, 1999b; Milovanov and Zelenyi, 2000; Leubner, 2004; Borges et al., 2002; Livadiotis and McComas, 2009, etc

Kappa distributions in the magnetosphere of the Earth

Fitting the particle fluxes in the magnetosphere of the Earth [Christon et al., 1991; Pisarenko et al., 2002; Wang et al., 2011; Lui, 2013, etc].

The field-aligned acceleration of auroral particles [Olsson and Janhunen, 1998; Dors and Kletzing, 1999; Ermakova and Antonova, 2007; Antonova et al., 2012],

The transverse acceleration of ions during substorm injections [Birn et al., 1997; Zaharia et al., 2000]

The theory of formation of the inverted-V structures [Antonova et al. 2003; Ermakova et al., 2006]

The values of plasma pressure from the DMSP satellites [Wing and Newell, 1998; Wing et al., 2013]

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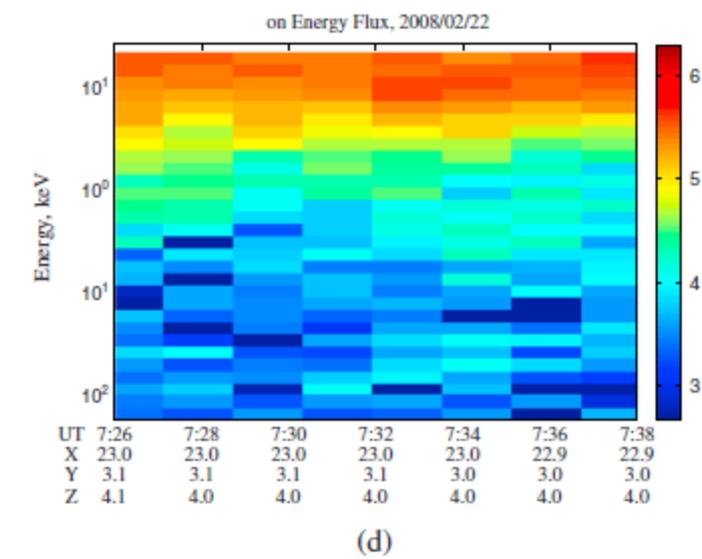
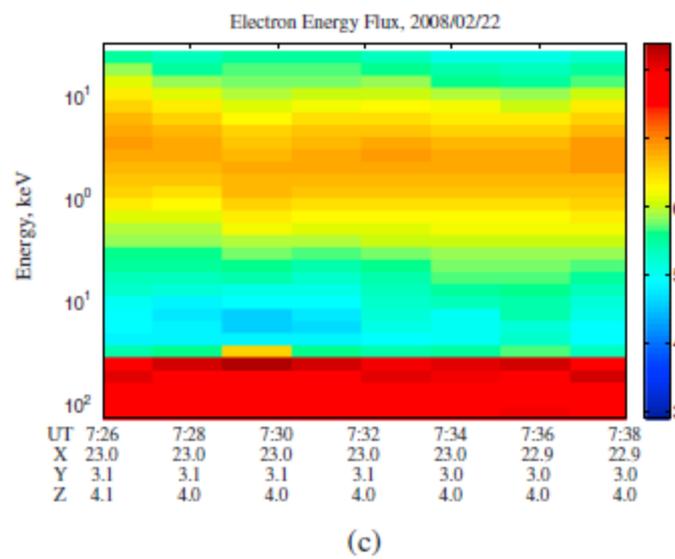
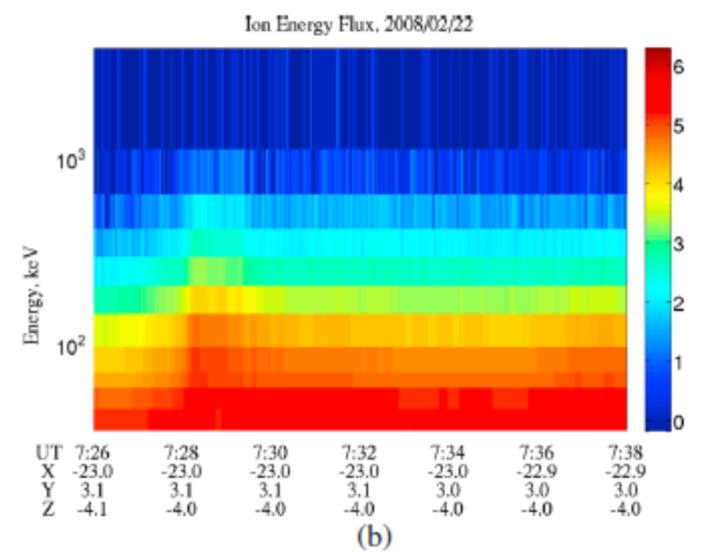
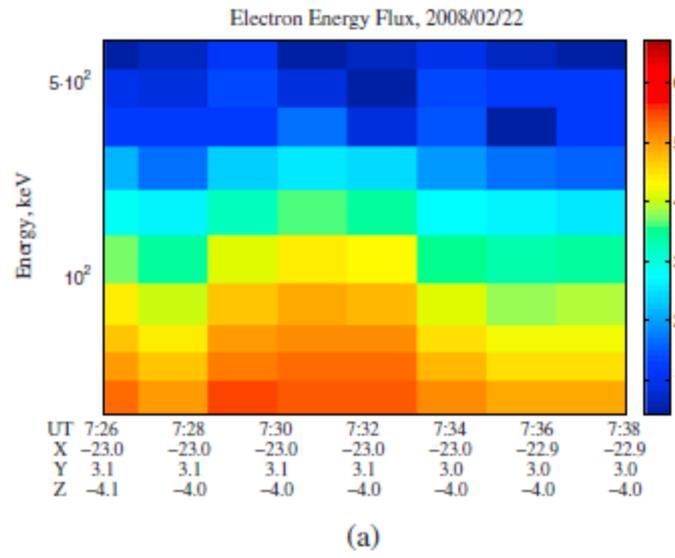
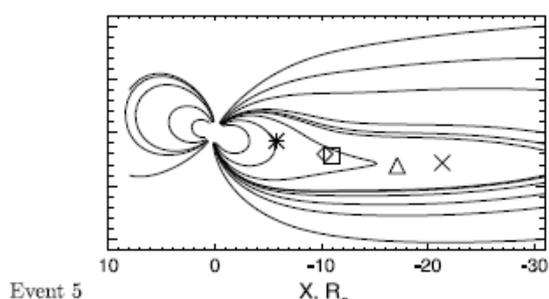
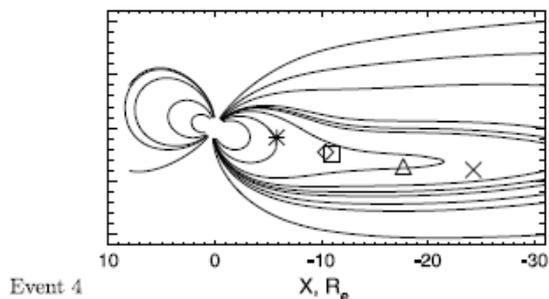
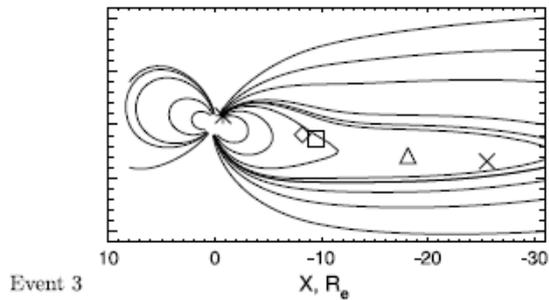
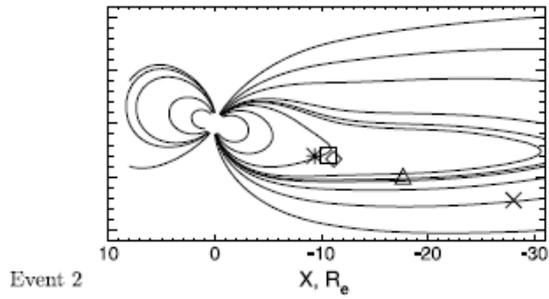
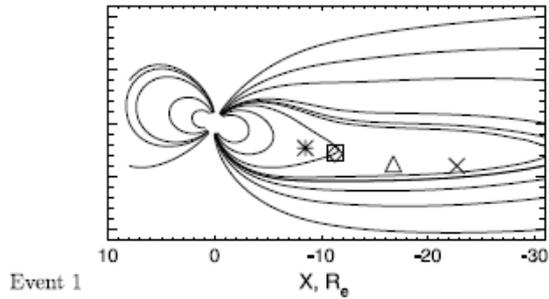
The transverse acceleration of ions during substorm injections [Birn et al., 1997; Zaharia et al., 2000]

The theory of formation of the inverted-V structures [Antonova et al. 2003; Ermakova et al., 2006]

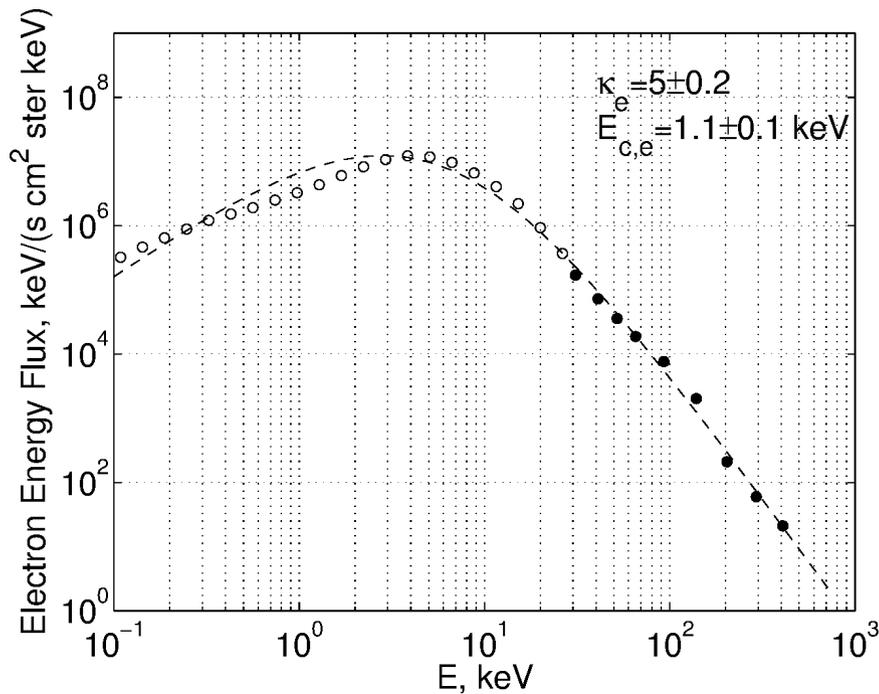
The values of plasma pressure from the DMSP satellites [Wing and Newell, 1998; Wing et al., 2013]

Do exist any radial dependence of kappa parameters on the distance toward the tail in the plasma sheet?

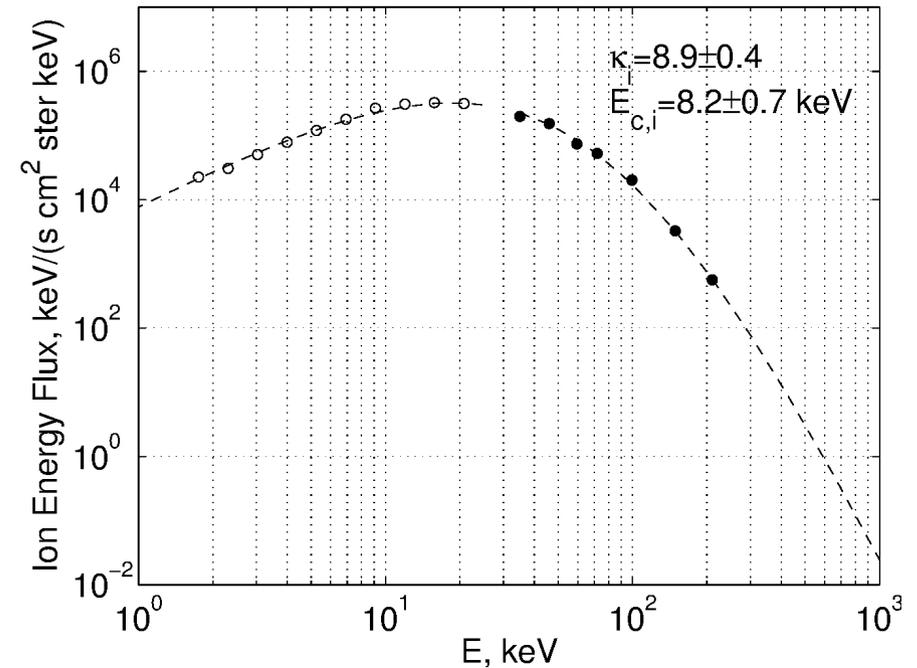
Stepanova and Antonova, JGR, doi:10.1002/2014JA020684.



Number fluxes for five satellites located in the plasma sheet were fitted by kappa distribution functions:



(a)

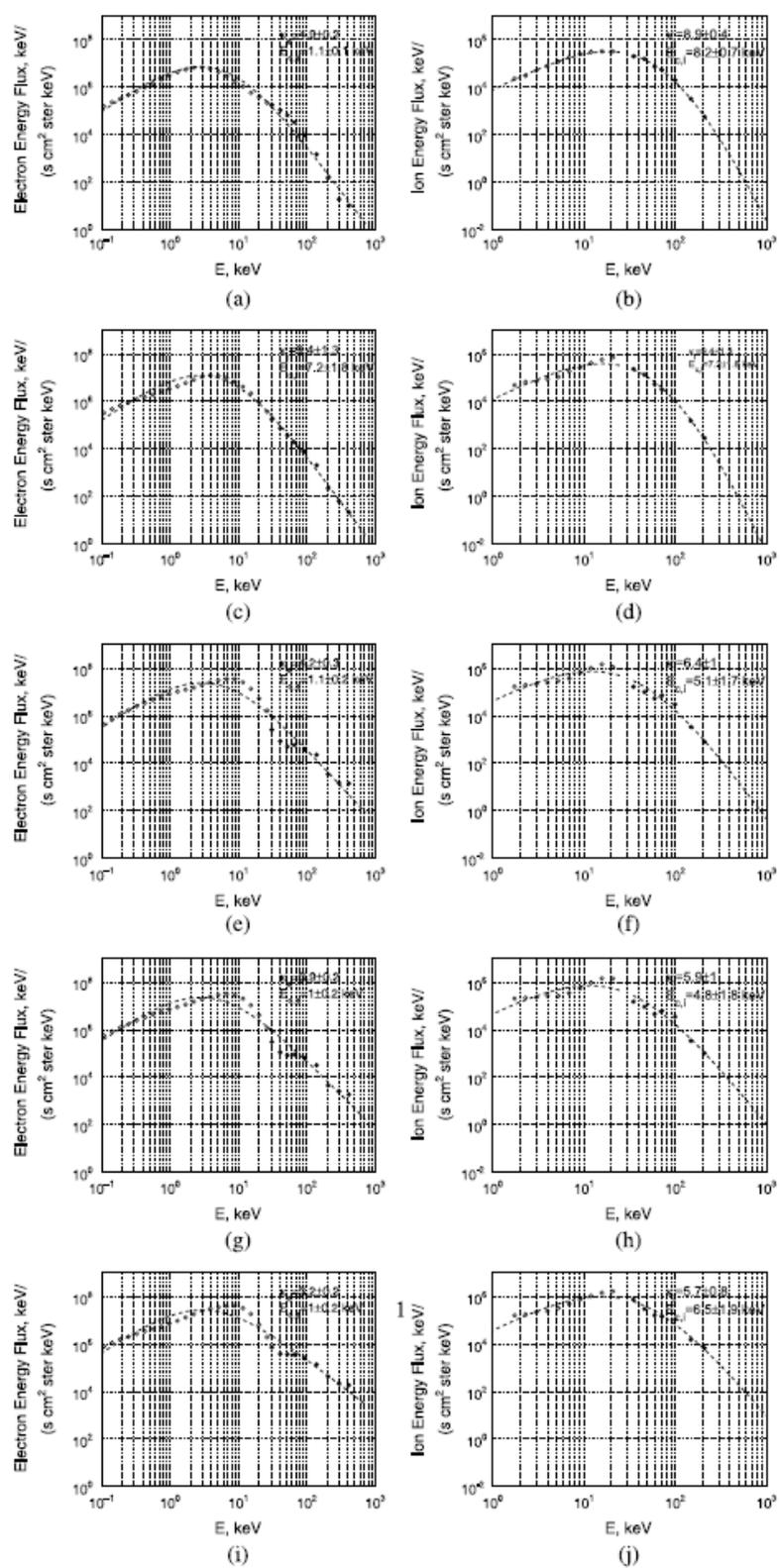


(b)

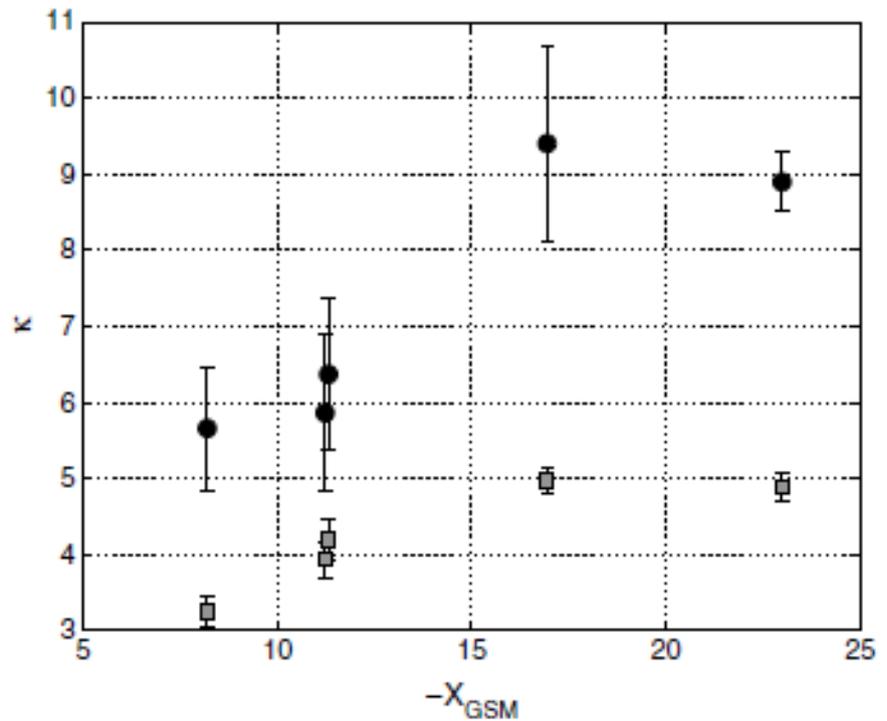
$$F_{e,j}(E) = \frac{1}{\pi} \frac{n_{e,j}}{\sqrt{2\pi m_{e,j}}} \frac{E^2}{E_{c,e,j}^{3/2}} \frac{\Gamma(\kappa_{e,j})}{\Gamma(\kappa_{e,j} - 1/2) \sqrt{\kappa_{e,j}}} \left[1 + \frac{E}{\kappa E_{c,e,j}} \right]^{-\kappa_{e,j}-1} \quad (3)$$

where $n_{e,j}$ is the electron (ion) density, $m_{e,j}$ is the electron (ion) mass, E is the particle energy, $E_{c,e,j}$ is the electron (ion) energy of the peak differential number flux, and $\kappa_{e,j}$ is the spectral index characterizing the electron (ion) distribution.

Combined ESA and SST measurements. Some low energy ESA and high energy SST channels were discarded. Final range: 1.75 and 210 keV (ions), 0.362 and 203.5 keV (electrons).

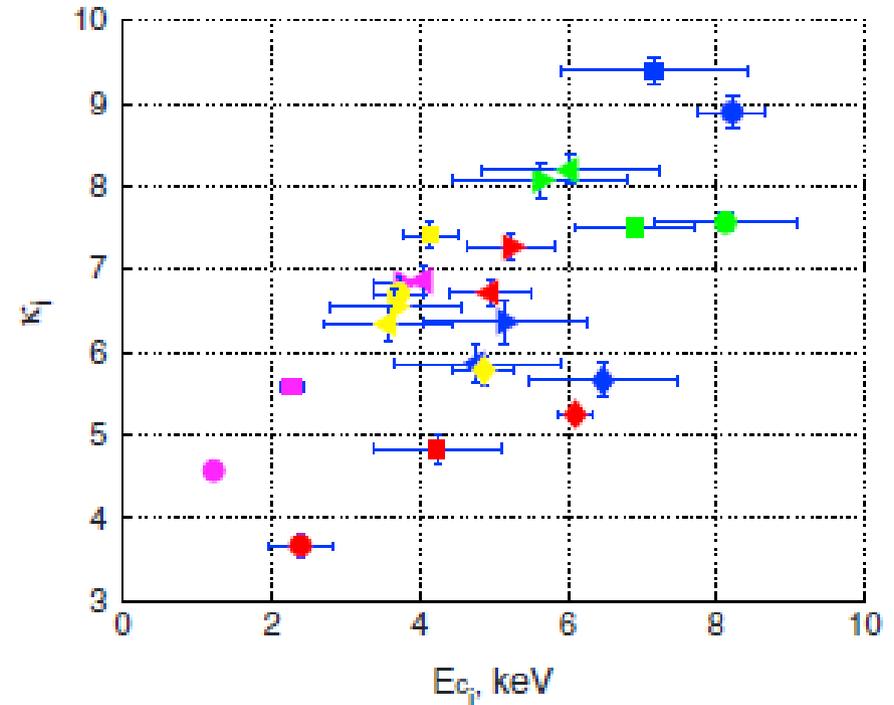
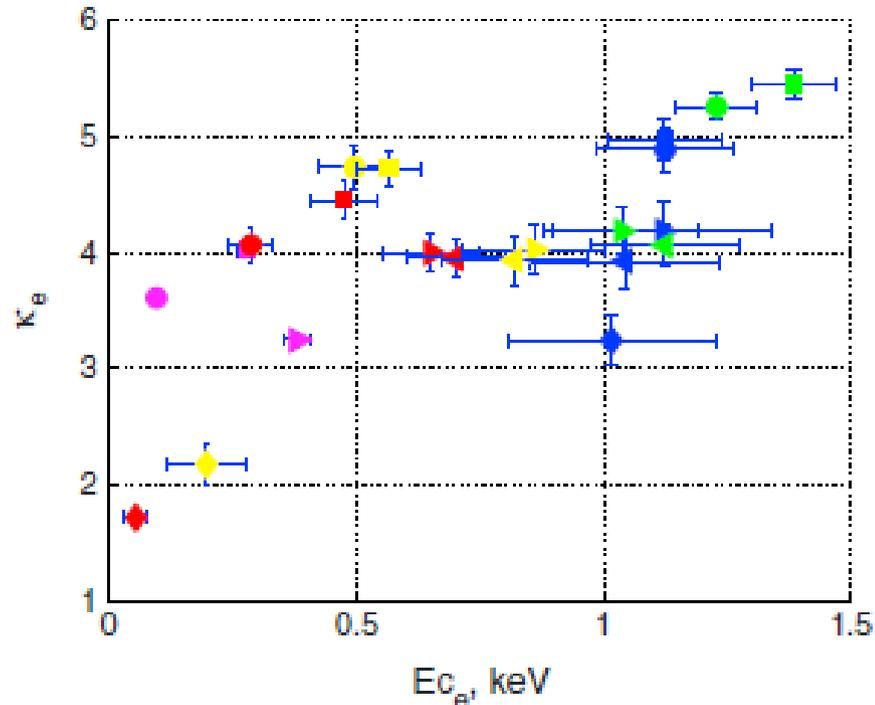


Averaged electron and ion energy flux spectra, measured on 22 February 2008 between 7:26 and 7:38 UT and fitted by kappa distribution: (a, b) THB, XGSM = -22.9RE, (c, d) THC, XGSM = -16.9RE, (e, f) THD, XGSM = -11.3RE, (g, h) THE, XGSM = -11.2RE, and (i, j) THA, XGSM = -8.3RE.



Evolution of κ index with the distance from the Earth on 22 February 2008 between 7:26 and 7:38 UT for ions (black circles) and electrons (grey squares).

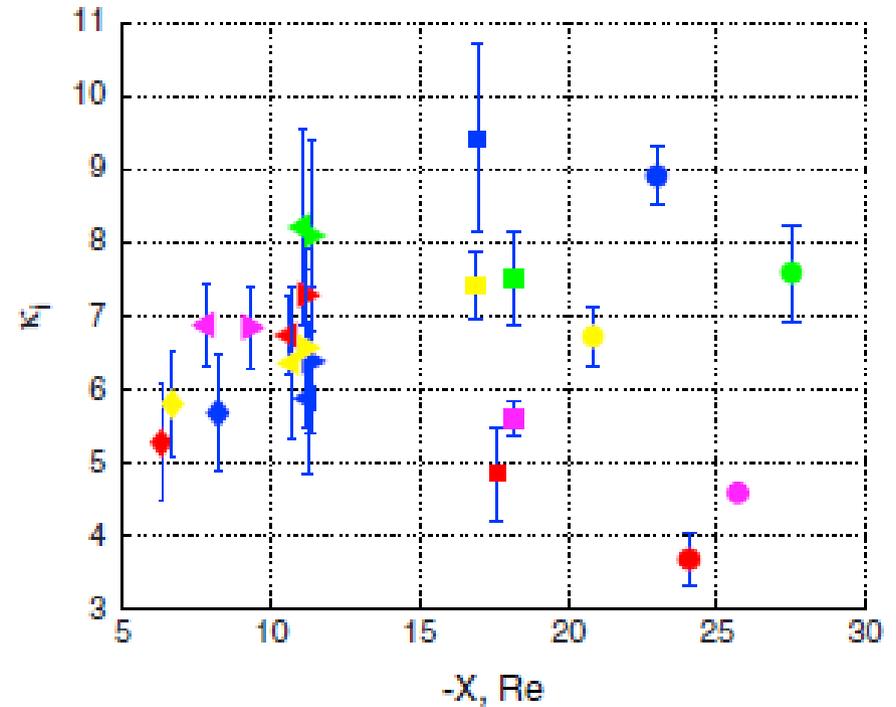
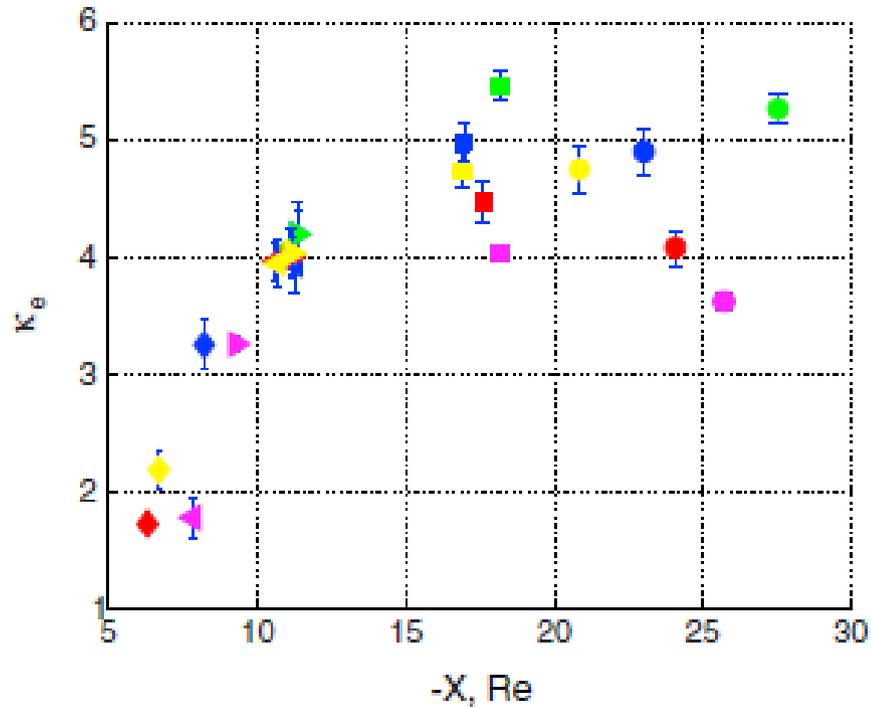
Relation between the kappa indexes and the core energy



Colors indicate the event numbers (1 = blue, 2 = green, 3 = magenta, 4 = red, and 5 = yellow). Symbols indicate the satellite used (THB = circle, THC = square, THD = right-pointing triangle, THE = left-pointing triangle, and THA = diamond).

A relation between the values of κ and the core energy, in general, follows the statistical results obtained by Christon et al. [1989]

Variation of the kappa indexes with the distance toward the tail



Colors indicate the event numbers (1 = blue, 2 = green, 3 = magenta, 4 = red, and 5 = yellow). Symbols indicate the satellite used (THB = circle, THC = square, THD = right-pointing triangle, THE = left-pointing triangle, and THA = diamond).

Hypothesis about particle acceleration, loss and transport

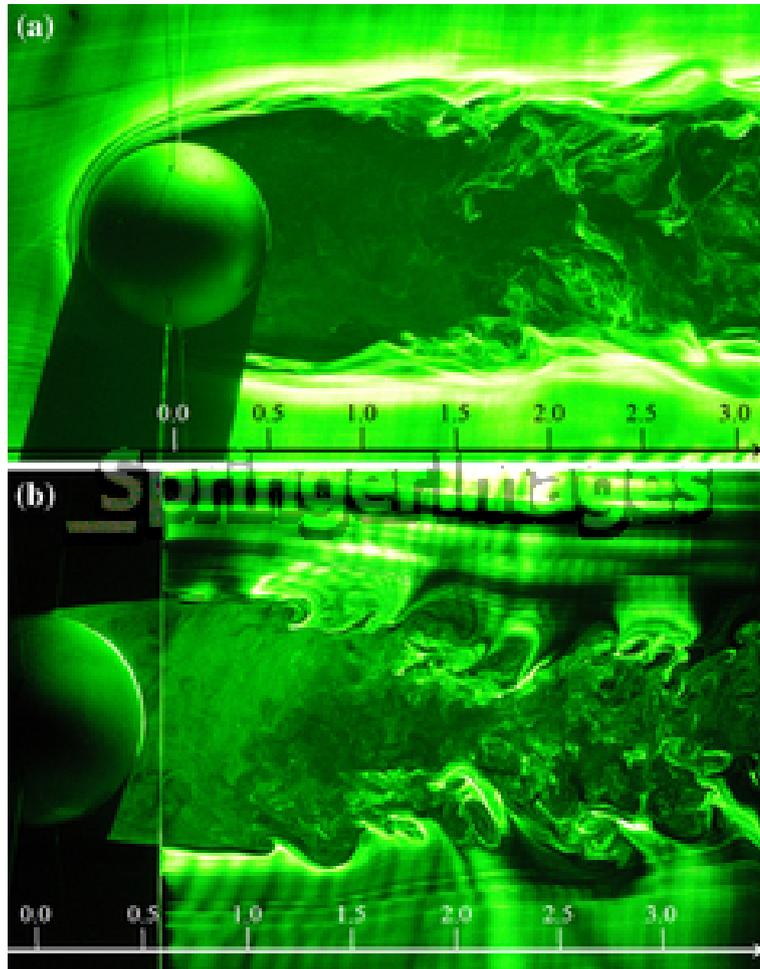
The source of the particle acceleration is located near the Earth.
Agrees with works of Denton and Cayton [2011], Borovsky and Denton [2011], Reeves et al. [2013].

The relaxation of the distribution function to a Maxwellian is due to diffusion in velocity space [Collier, 1999]

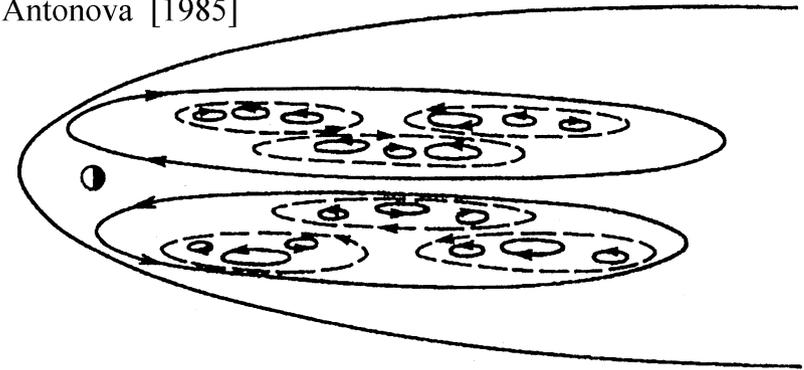
Net transport toward the tail?

Transports having mainly earthward direction: regular transport due to the dawn-dusk electric field, BBFs, dipolarization fronts.

Turbulent transport in the plasma sheet

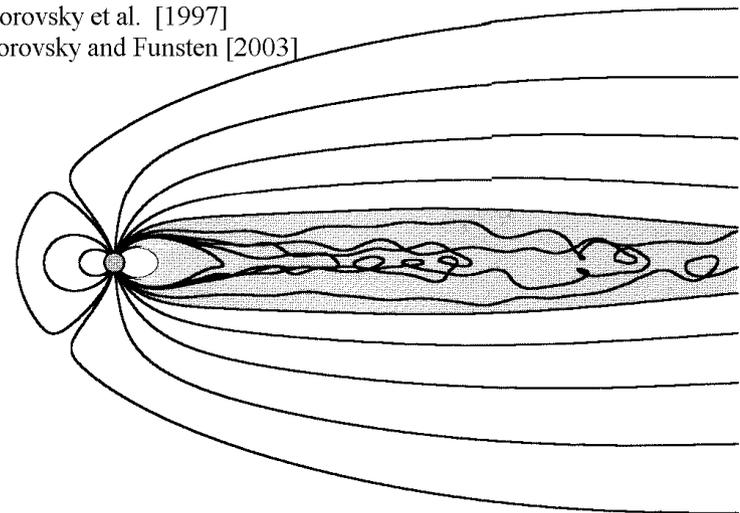


Antonova [1985]



Borovsky et al. [1997]

Borovsky and Funsten [2003]



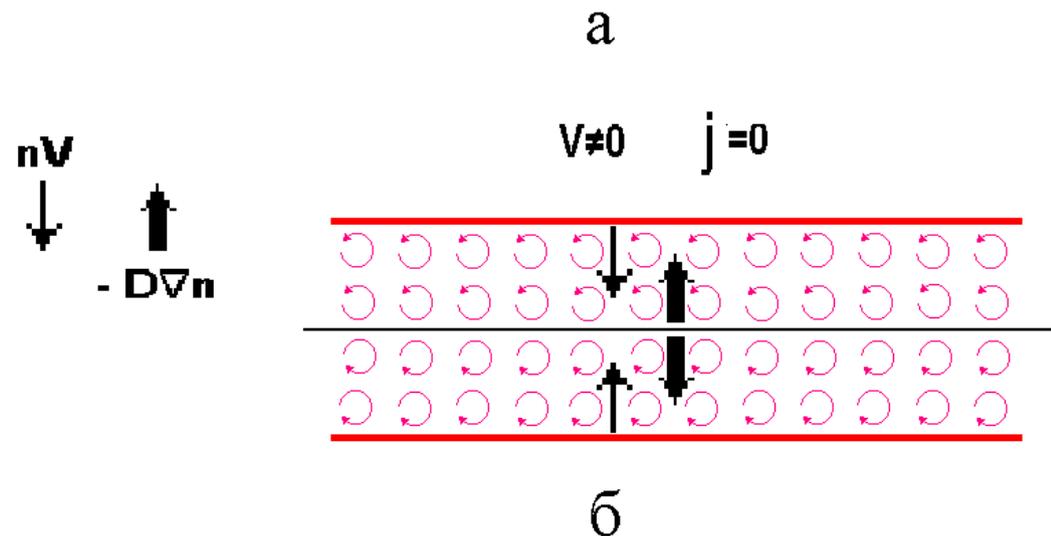
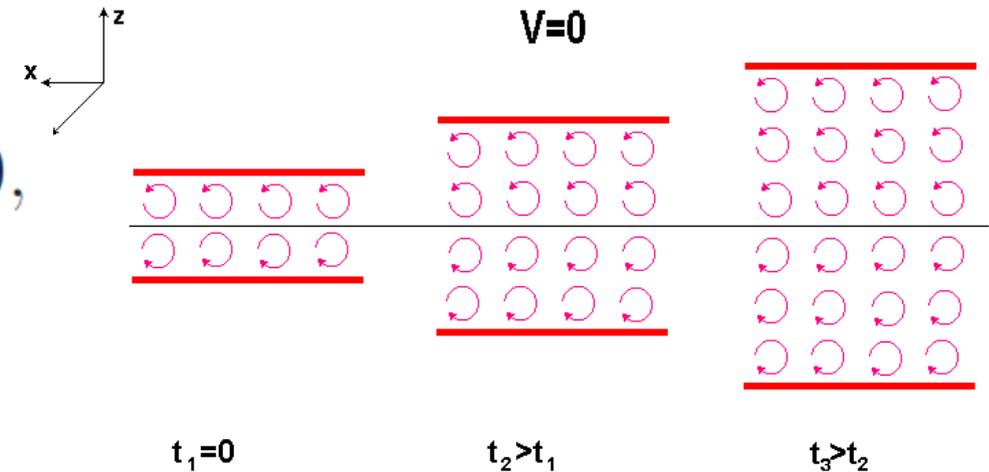
Even for laminar solar wind, we would expect the formation of a turbulent wake behind an obstacle, considering the very high values of Reynolds number ($> 10^{10}$, Borovsky and Funsten, 2003).

How to stabilize the turbulent plasma sheet?

$$\Gamma = \langle n\mathbf{V} \rangle = n_0\mathbf{V}_0 - D\nabla n = 0,$$

A balance between the regular and turbulent transports (Antonova and Ovchinnikov, 1996, 1997, 1999)

The total pressure balance across the geotail (Michalov et al. [1968], Stiles [1978], Spence et al. [1989], Tsyganenko [1990], Baumjohann et al. [1990], Kistler et al. [1993], Petrukovich [1999], Tsyganenko and Mukai [2003])



The regular plasma transport, which is transverse to the plasma sheet and related to the dawn-dusk electric field, is compensated by the eddy diffusion turbulent transport.

$$\Gamma = \langle n\mathbf{V} \rangle = n_0\mathbf{V}_0 - D\nabla n = 0, \quad (1)$$

where $\Gamma = \langle n\mathbf{V} \rangle$ is the total number flux, $n_0\mathbf{V}_0$ is the number flux due to regular transport, and $D\nabla n$ is the number flux due to the turbulent transport. Here n and \mathbf{V} are the plasma number density and velocity, n_0 and \mathbf{V}_0 are their average values, and D is the coefficient of eddy diffusion transverse to the plasma sheet.

Assuming existence of a total pressure balance across the plasma sheet, and constant ion temperature across the sheet:

$$\frac{l}{p} \frac{dp}{dz} = f(b) \quad (2)$$

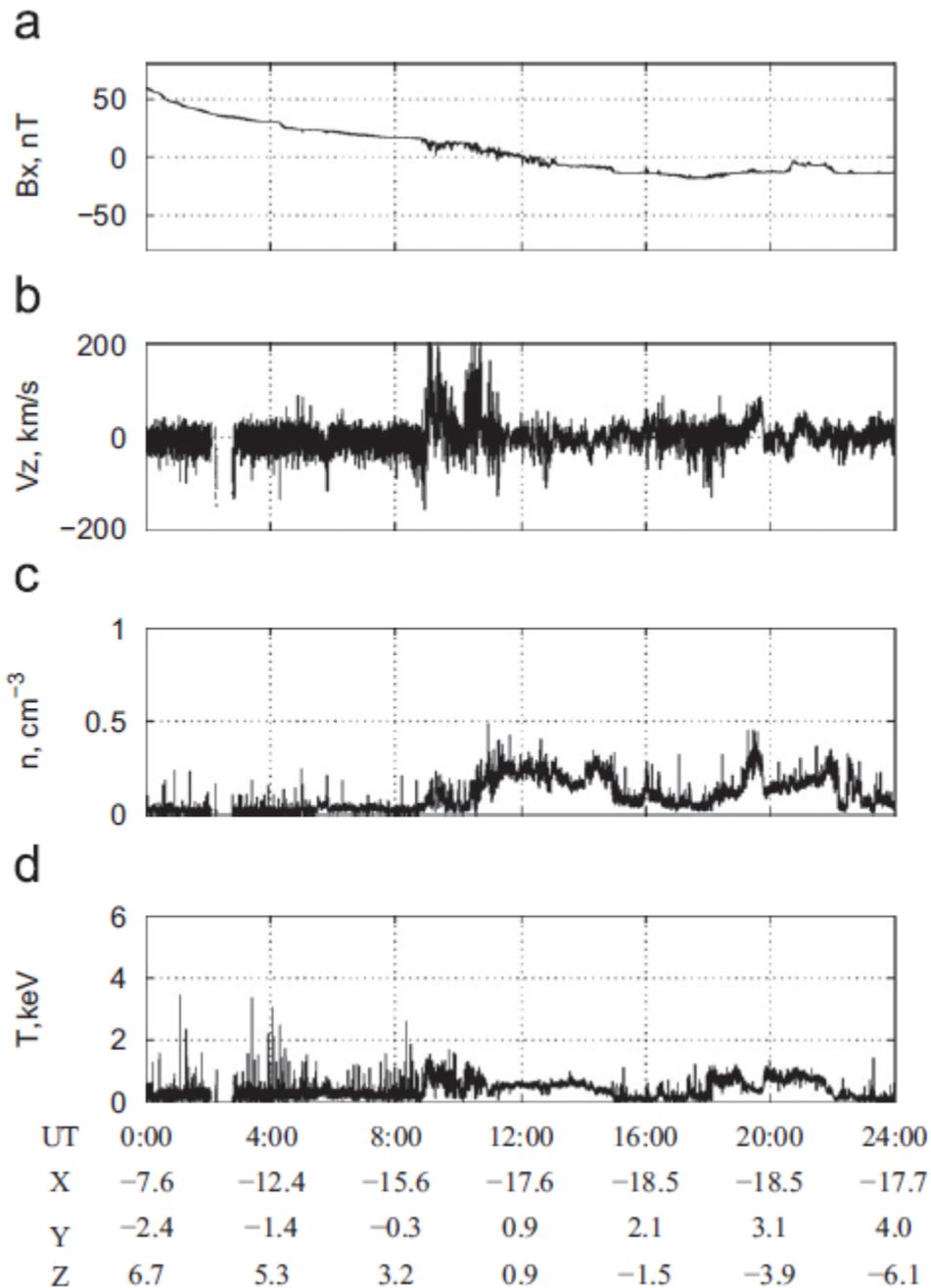
where $b = B/B_L$, B_L is the magnetic field in the tail lobes, $f(b) = lV_z(b)/D(b)$, $l = (D/V_z)|_{B=B_L}$ is the characteristic scale, and D is the coefficient of eddy diffusion.

For $D \sim B^{-2}$ and $f(b) \sim b$. Taking into consideration that the total pressure across the tail is constant, i.e. $p = p_0(1 - b^2)$, we integrate (2) to obtain a Harris-type solution for the geomagnetic field,

$$B = B_L \tanh(z/2l). \quad (3)$$

The plasma pressure varies across the sheet as

$$p = p_0 \cosh^{-2}(z/2l). \quad (4)$$



Cluster vertical crossing

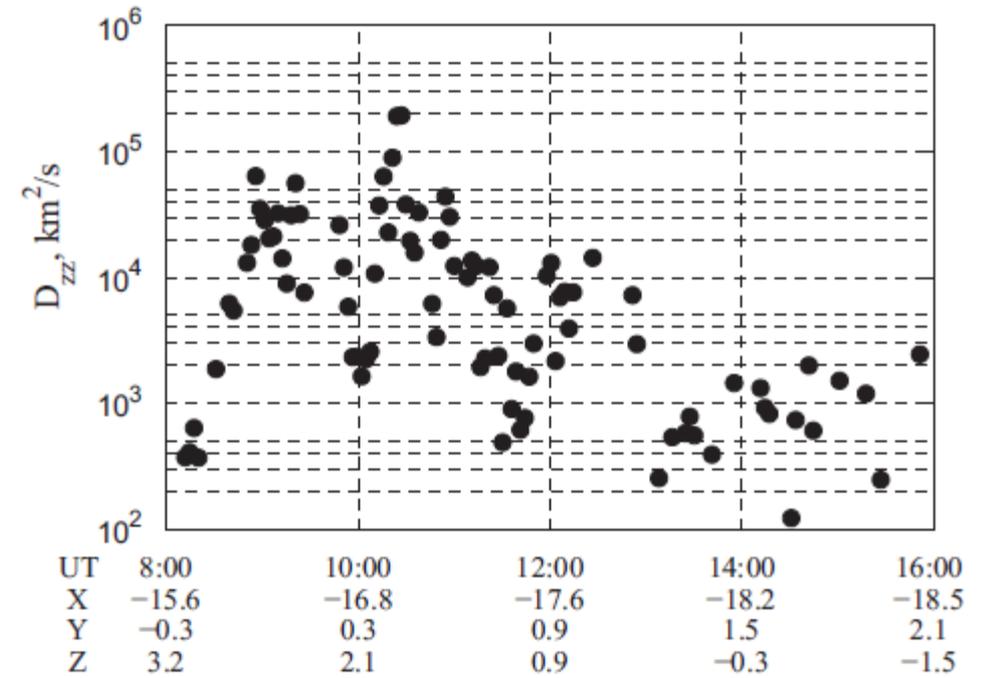


Fig. 2. Variation of eddy-diffusion coefficient D in the direction Z across the plasma sheet during quiet geomagnetic conditions.

September 12, 2004

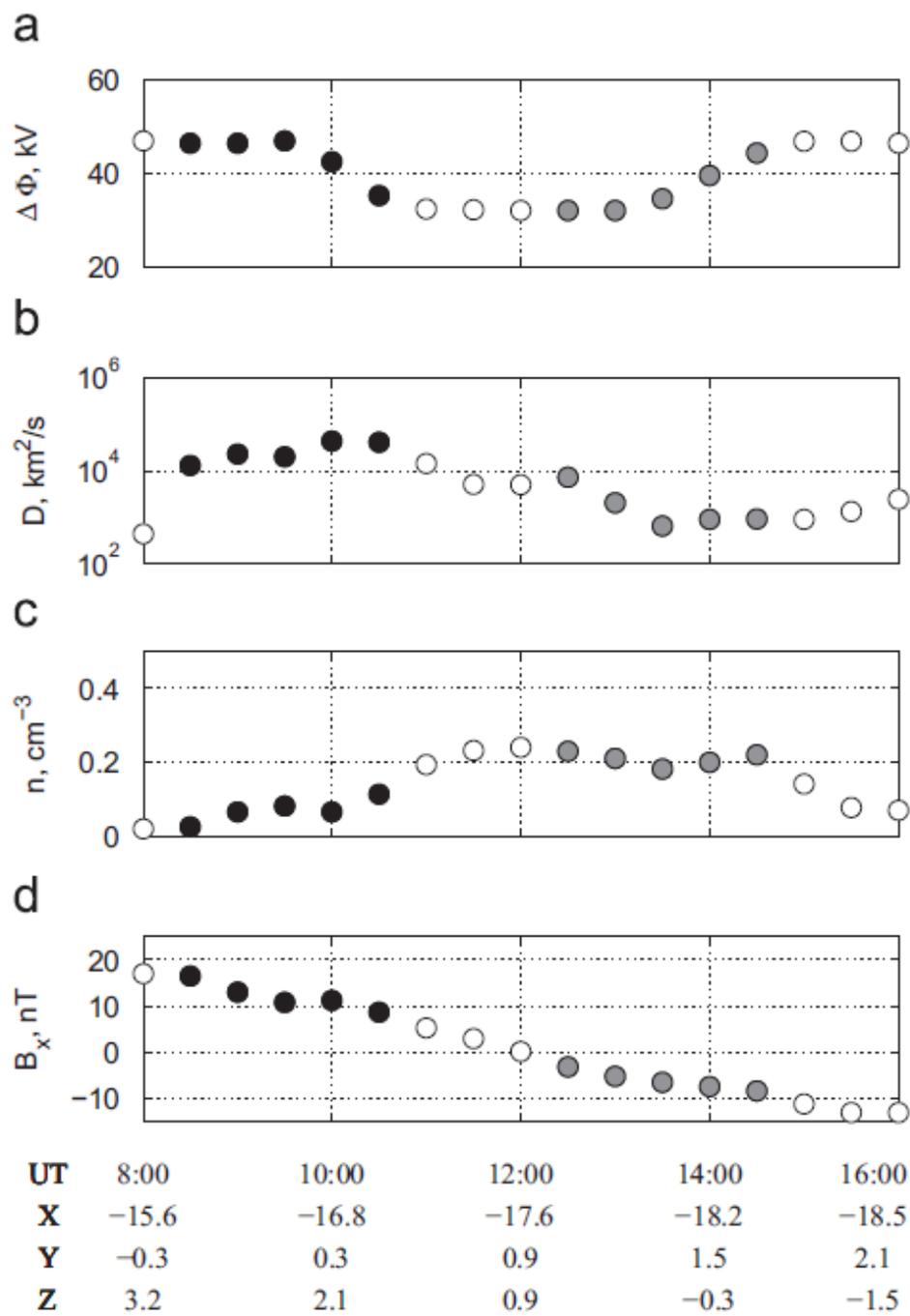


Fig. 3. From top to bottom: averaged values of the polar cap potential difference (a), Z component of the eddy diffusion coefficient (b), the ion number density (c), and the X component of the geomagnetic field (d), in the GSE coordinate system for September 12, 2004 event.

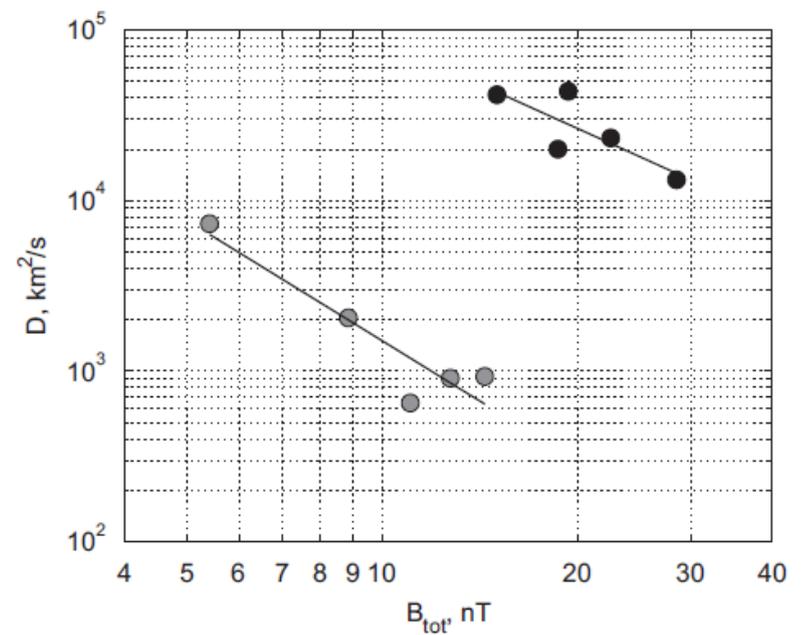


Fig. 4. Variation of the eddy-diffusion coefficient vs. the absolute value of the geomagnetic field, the circle color is the same as for Fig. 3. The lines represent the best fit, $D(B) = (4.5 \pm 0.8) \cdot 10^6 \cdot B^{-1.7 \pm 0.7} \text{ km}^2/\text{s}$ for $\Delta\Phi = 46 \text{ kV}$ while in the case of $\Delta\Phi = 32 \text{ kV}$ it is $D(B) = (0.33 \pm 0.03) \cdot 10^6 \cdot B^{-2.3 \pm 0.5} \text{ km}^2/\text{s}$.

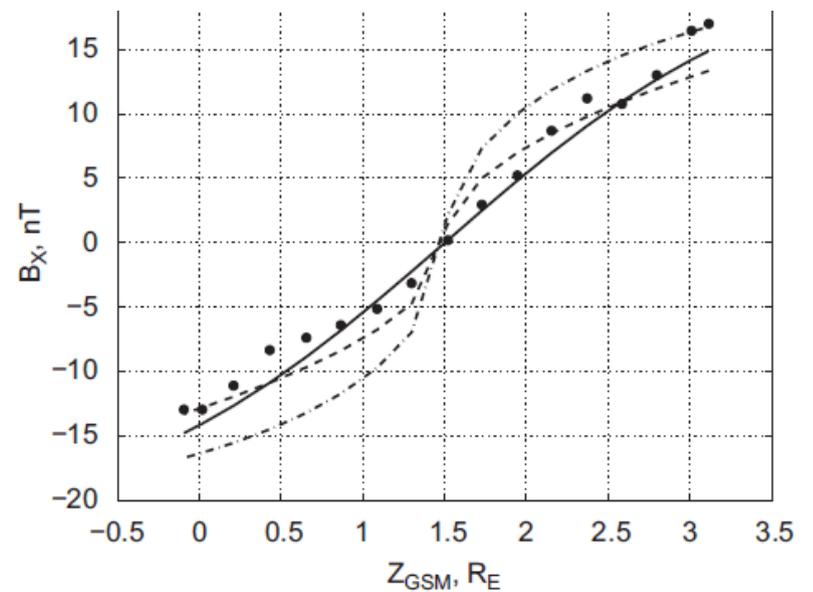
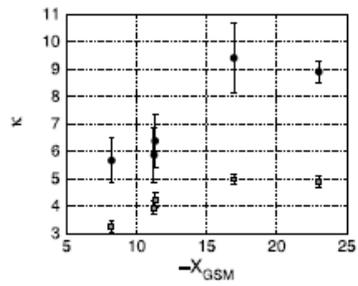
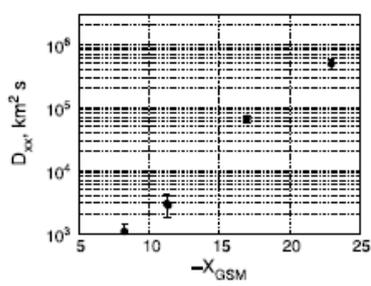


Fig. 5. The X-component of the magnetic field B_x vs. Z (dots) fitted by the expression (4) (solid line), fitted by (7) (dashed line, green online). The curve given by (7) with a realistic value of $2I=2R_E$ (dashed-dotted line). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

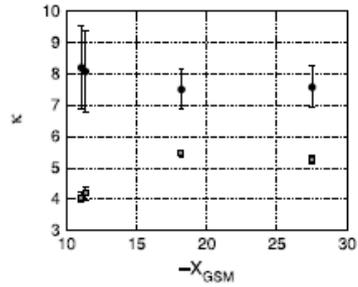
Is it possible to have a tailward turbulent transport?



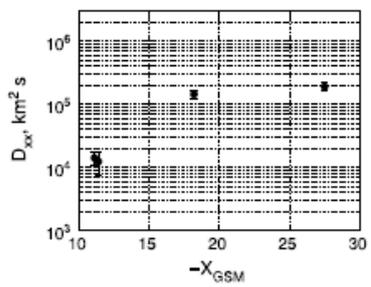
(a)



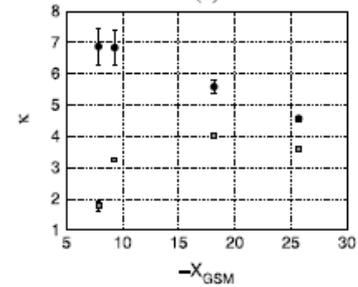
(b)



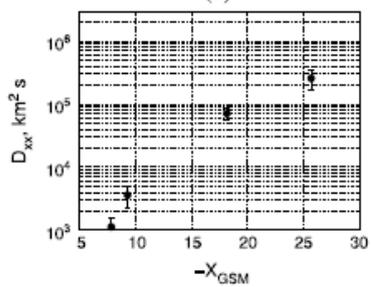
(c)



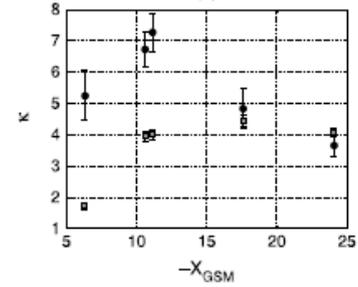
(d)



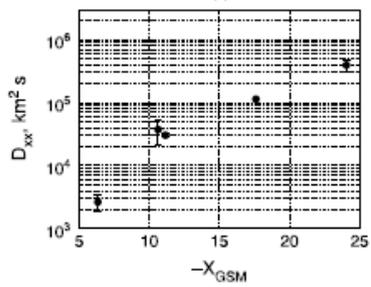
(e)



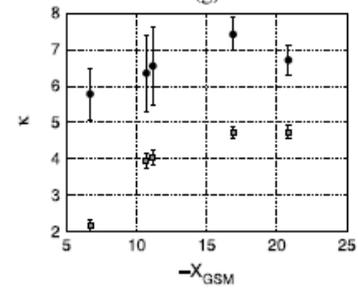
(f)



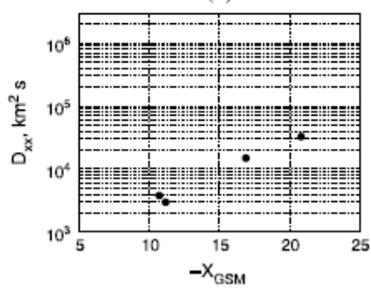
(g)



(h)



(i)

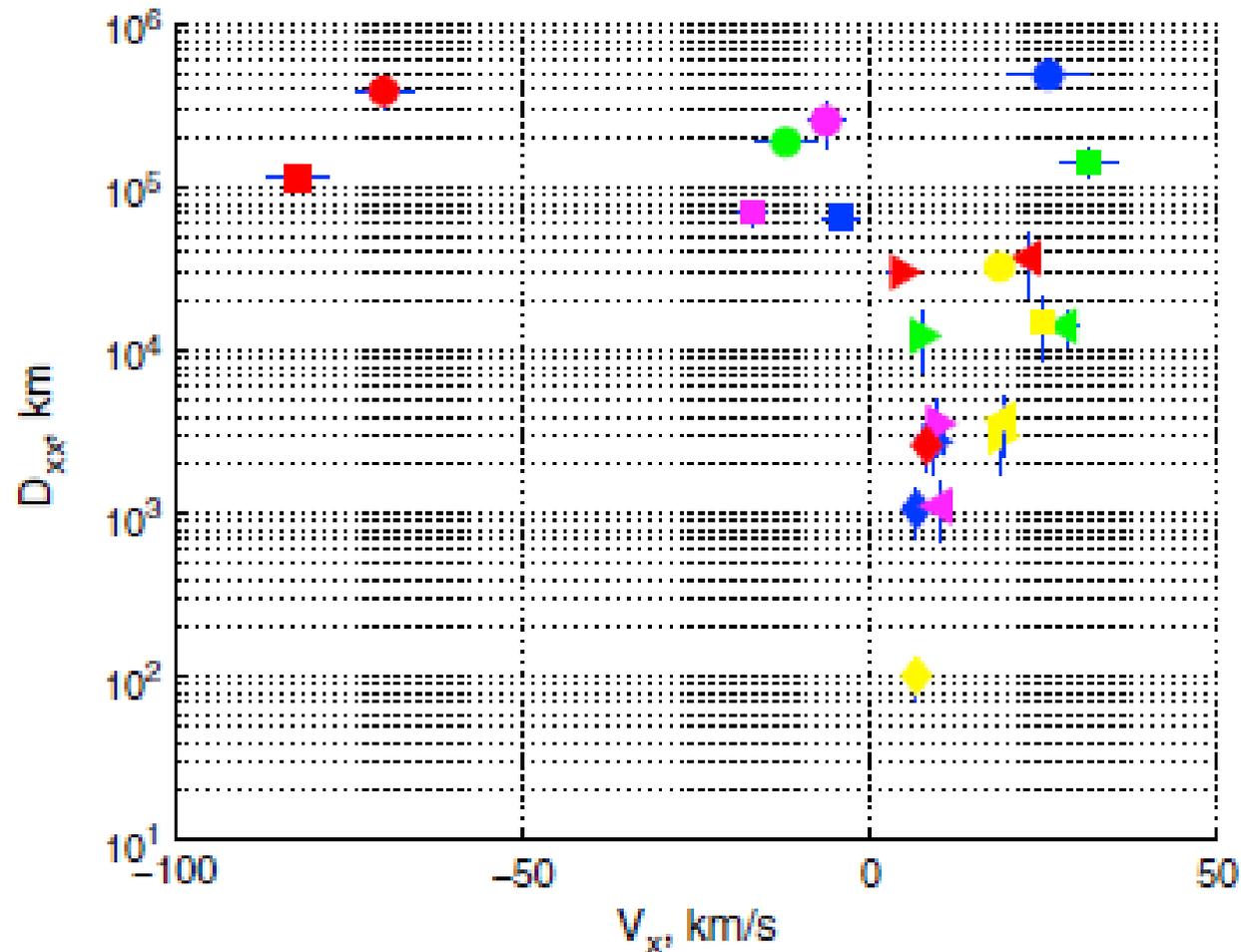


(j)

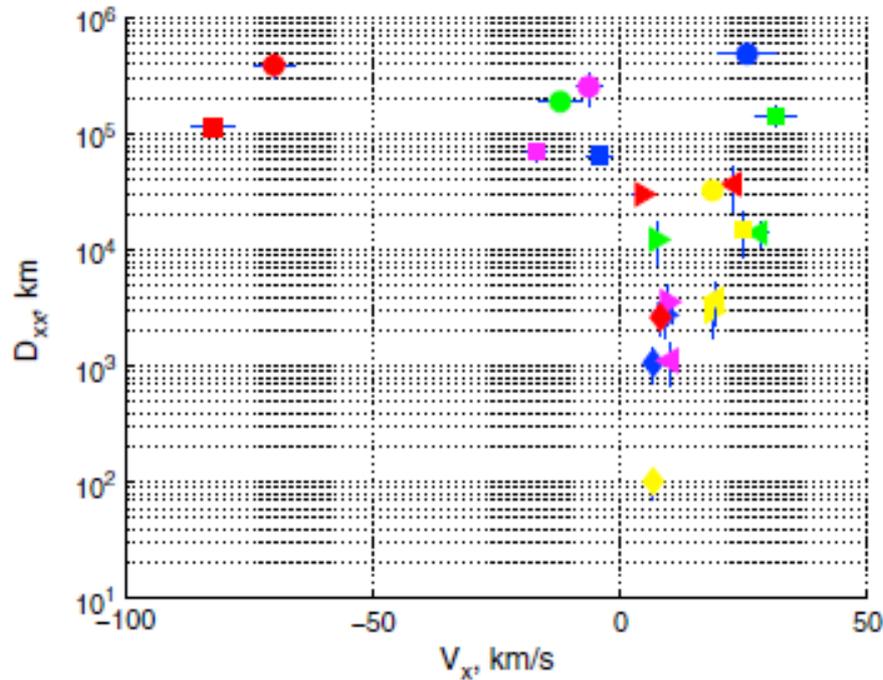
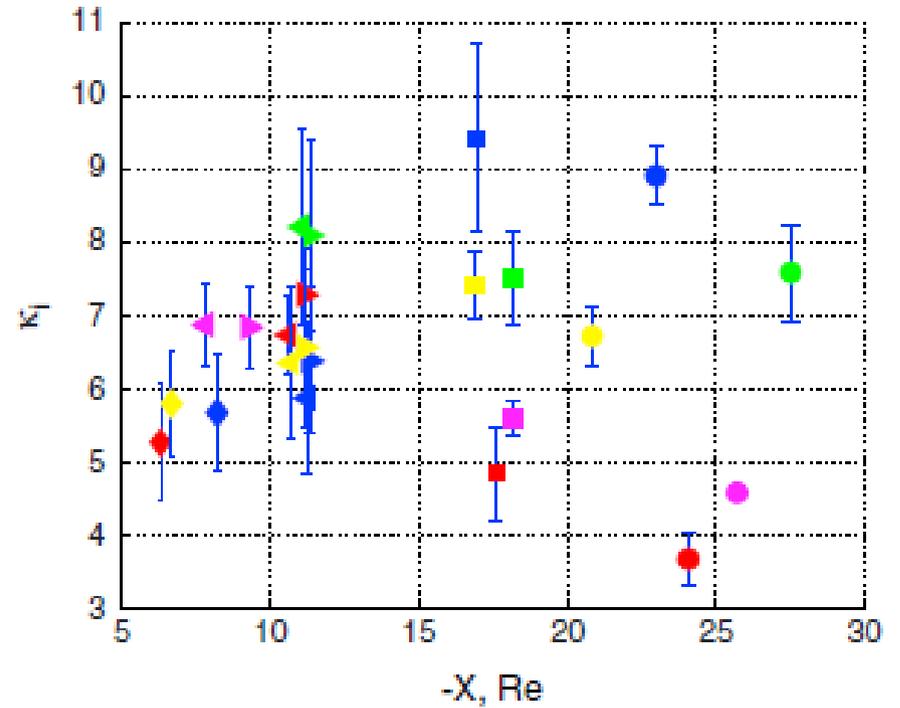
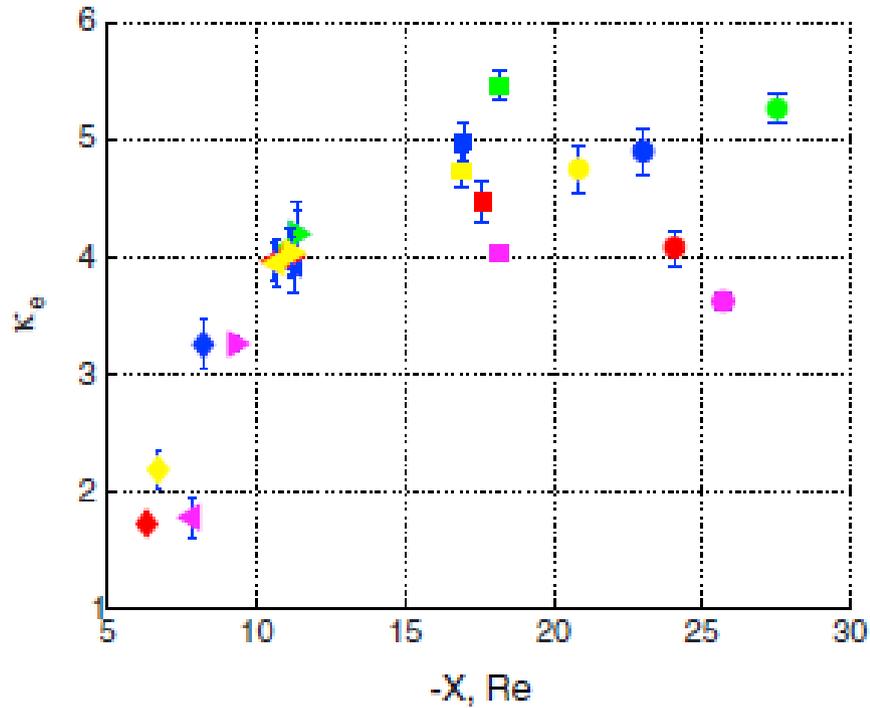
$$t_{diff} \approx \frac{\Delta L^2}{\langle D_{xx'} \rangle}$$

The characteristic times of eddy diffusion are about 3-12 hours.

What is happening with regular transport?



Colors indicate the event numbers (1 = blue, 2 = green, 3 = magenta, 4 = red, and 5 = yellow). Symbols indicate the satellite used (THB = circle, THC = square, THD = right-pointing triangle, THE = left-pointing triangle, and THA = diamond).



Deviation from the common trend is observed for the events when the regular transport was directed tailward (red and magenta diamond and square)

Conclusions

Under comparatively quiet geomagnetic conditions, [the parameters of the \$\kappa\$ approximation have a clear radial dependence](#), increasing in the tailward direction for the majority of events.

The action of [stochastic acceleration mechanisms near the Earth](#) leads to particle spectra hardening and to the appearance of suprathermal tails in particle fluxes, hence reducing the value of κ .

The relaxation of the κ distribution to the Maxwellian due to [diffusion in velocity space](#) takes place in the plasma sheet at the distances between 12 and 30 RE.

An increase in the values of κ with the distance to the tail requires the [net transport to be directed tailward](#). However, on average, the regular convection due to a dawn-dusk electric field is directed earthward, although even in our study we observed events as with earthward as with tailward average bulk velocity.

[Turbulent eddy diffusion is present in all events analyzed](#) The turbulent transport toward the tail takes a few hours, sufficient for the aging of distribution functions, observed in all events.

In the [events with the average bulk velocity pointed to the tail](#), both regular and turbulent mechanisms contributed to the net tailward transport, shortening the time available for relaxation. For these events we observed [more steep spectra in the distant plasma sheet](#).